

# Probabilistic Embedding Models

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Internal Blockchain Meeting  
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# Who Are Your Peers?

SINCE 1828

MENU

Merriam-Webster

peer

noun | \ˈpɪr\

Popularity: Top 10% of words

Examples: PEER in a sentence

f

t

g+

♥

CITE

G

Definition of PEER

1

one that is of equal standing with another : EQUAL <The band mates welcomed the new member as a peer.>; especially : one belonging to the same societal group especially based on age, grade, or status <teenagers spending time with their peers>

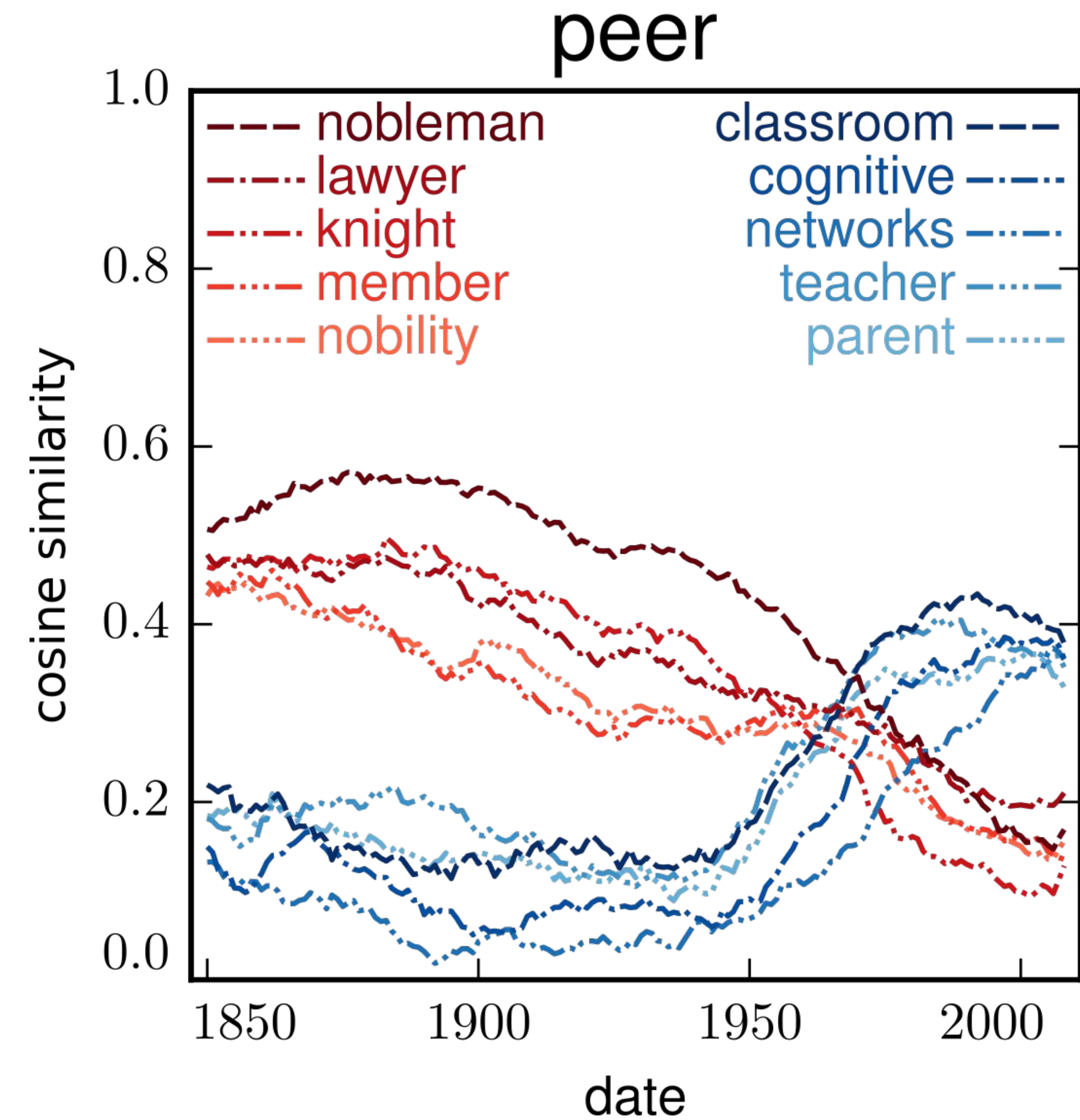
2

archaic : COMPANION

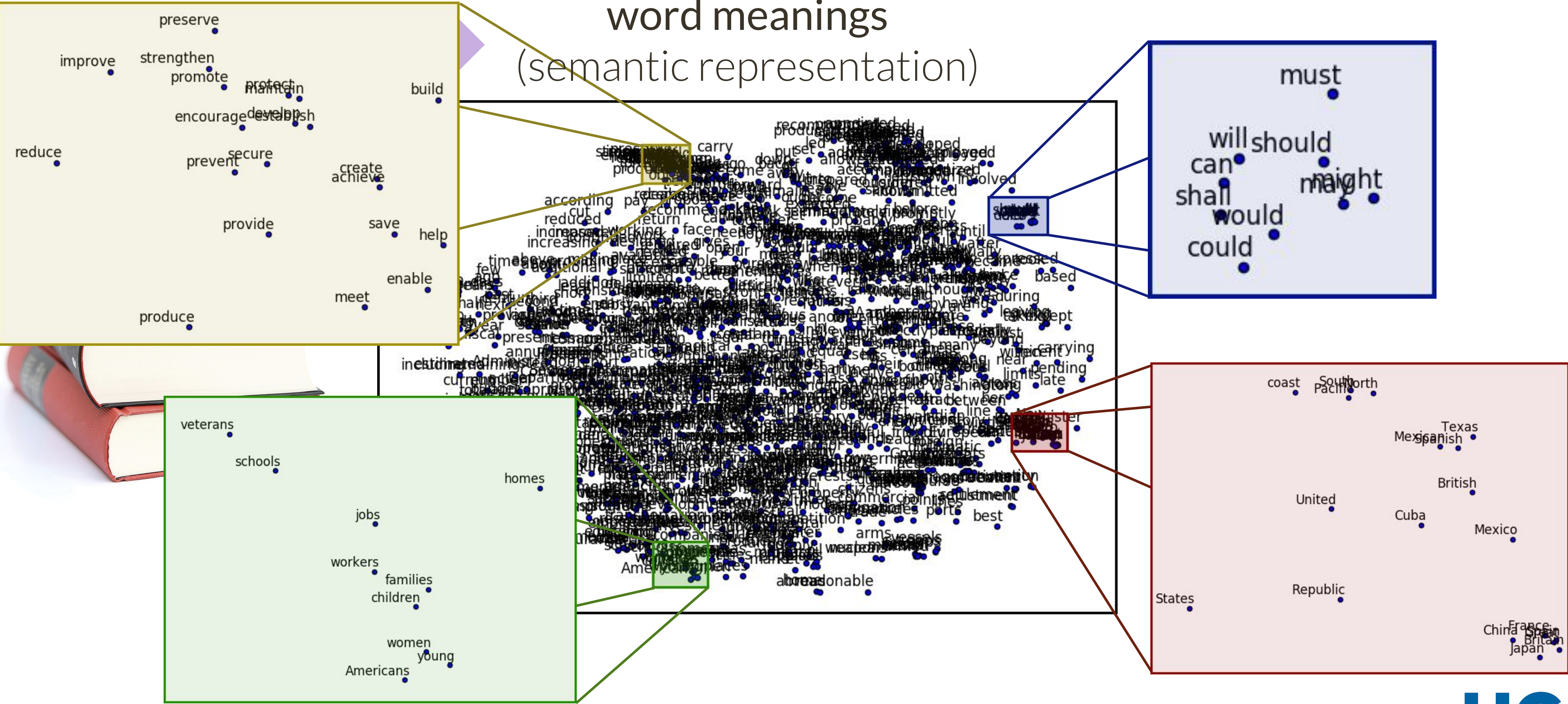
3

a : a member of one of the five ranks (as duke, marquess, earl, viscount, or baron) of the British peerage  
b : NOBLE 1 <Peers and commoners alike were shown the same courtesy.>

<https://www.merriam-webster.com/dictionary/peer>

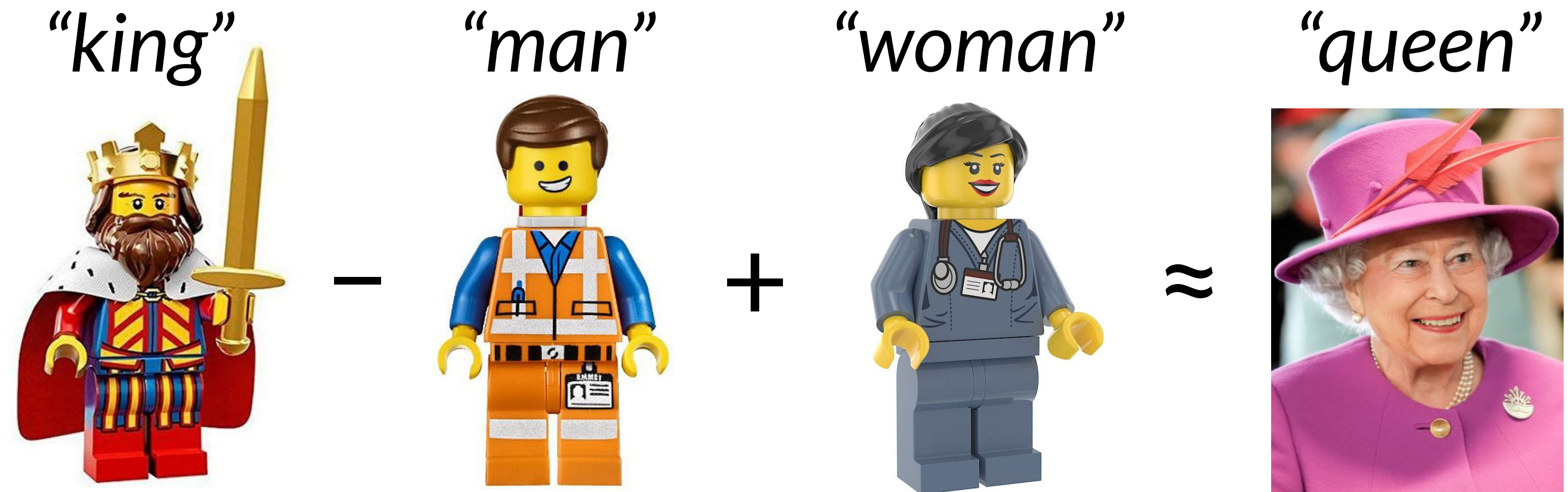


# Word Embeddings



# Word Embeddings

- Capture **semantic relations**:



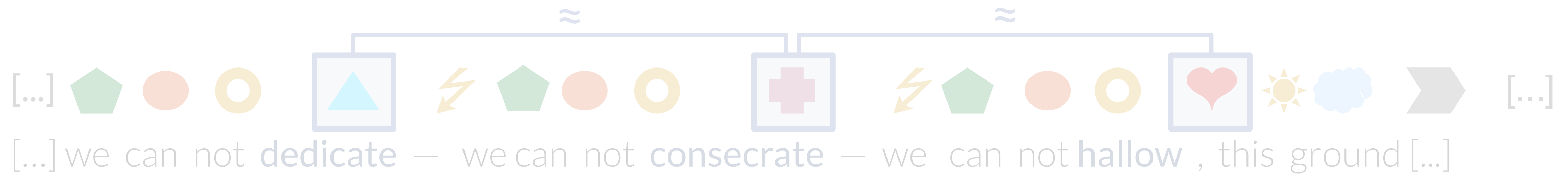
- Used for **transfer learning** in natural language processing, e.g., for **sentiment analysis**:



# Distributional Hypothesis

[Rubenstein & Goodenough, 1965; Sahlgren, 2008]

**Assumption:** Words that appear in similar contexts are similar in meaning.



(A. Lincoln, 1863)

**Semantic relations** between words:

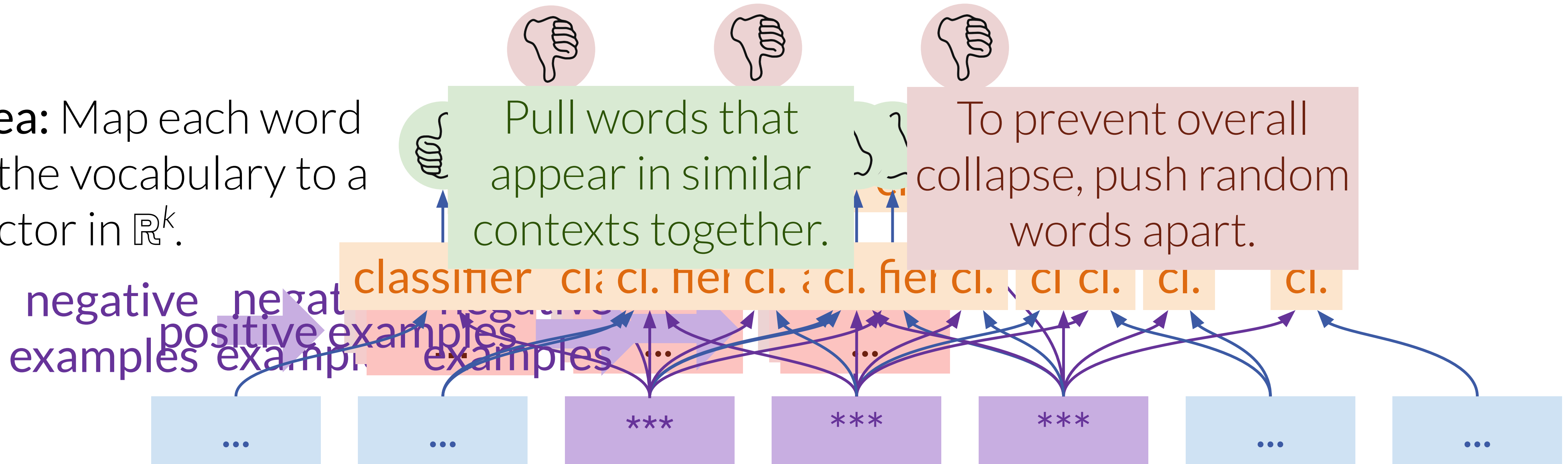


(Gen 5, 6 and Gen 5, 9)

# “Neural” Word Embeddings: word2vec

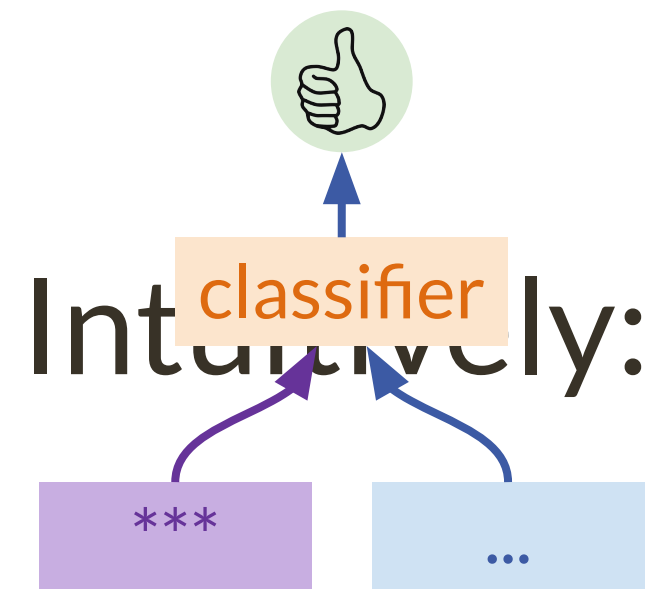
[Mikolov et al., ICLR 2013 & NIPS 2013]

**Idea:** Map each word in the vocabulary to a vector in  $\mathbb{R}^k$ .



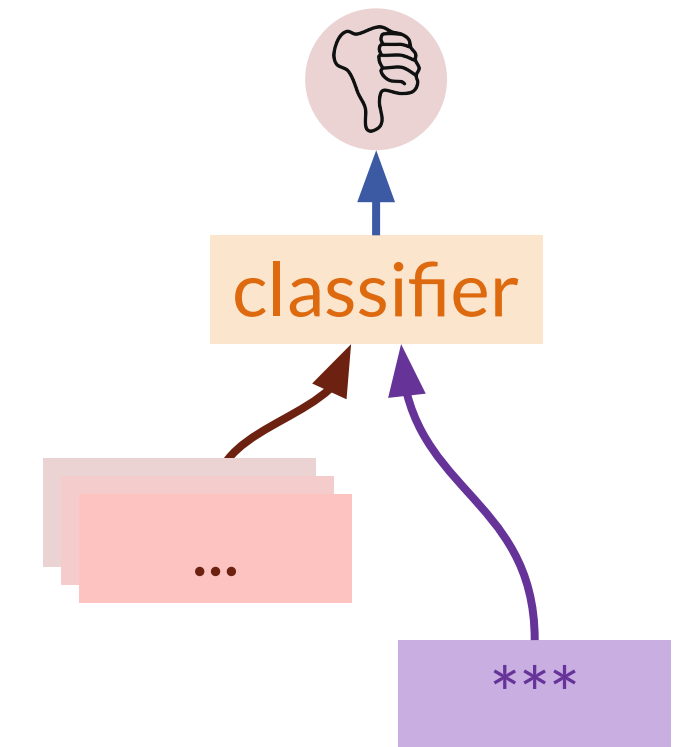
# “Neural” Word Embeddings: word2vec

[Mikolov et al., ICLR 2013 & NIPS 2013]



Pull words that appear in similar **contexts** together.

To prevent overall collapse, push random words apart.



Minimize loss function:  $\ell = - \sum_{(i,j) \in \text{pos.}} \log \sigma(u_i^\top v_j) - \sum_{(i,j) \in \text{neg.}} \log \sigma(-u_i^\top v_j)$

word embedding  
(vector in  $\mathbb{R}^k$ )

context embedding  
(vector in  $\mathbb{R}^k$ )

# Our Extension: Dynamic Word Embeddings

[Bamler & Mandt, ICML 2017]

“Computer” in 1961



© 20<sup>th</sup> century FOX

“Computer” today



# Detecting Subtle Changes Over Time

[Bamler & Mandt, ICML 2017]

## Naive idea:

Fit individual embedding vector for each word and each year.

## Problem:

Only few data **per word & year**.  
→ *small signal/noise ratio*

Our Solution:

1999

probabilistic version of word embeddings

+

probabilistic model of the dynamics

+

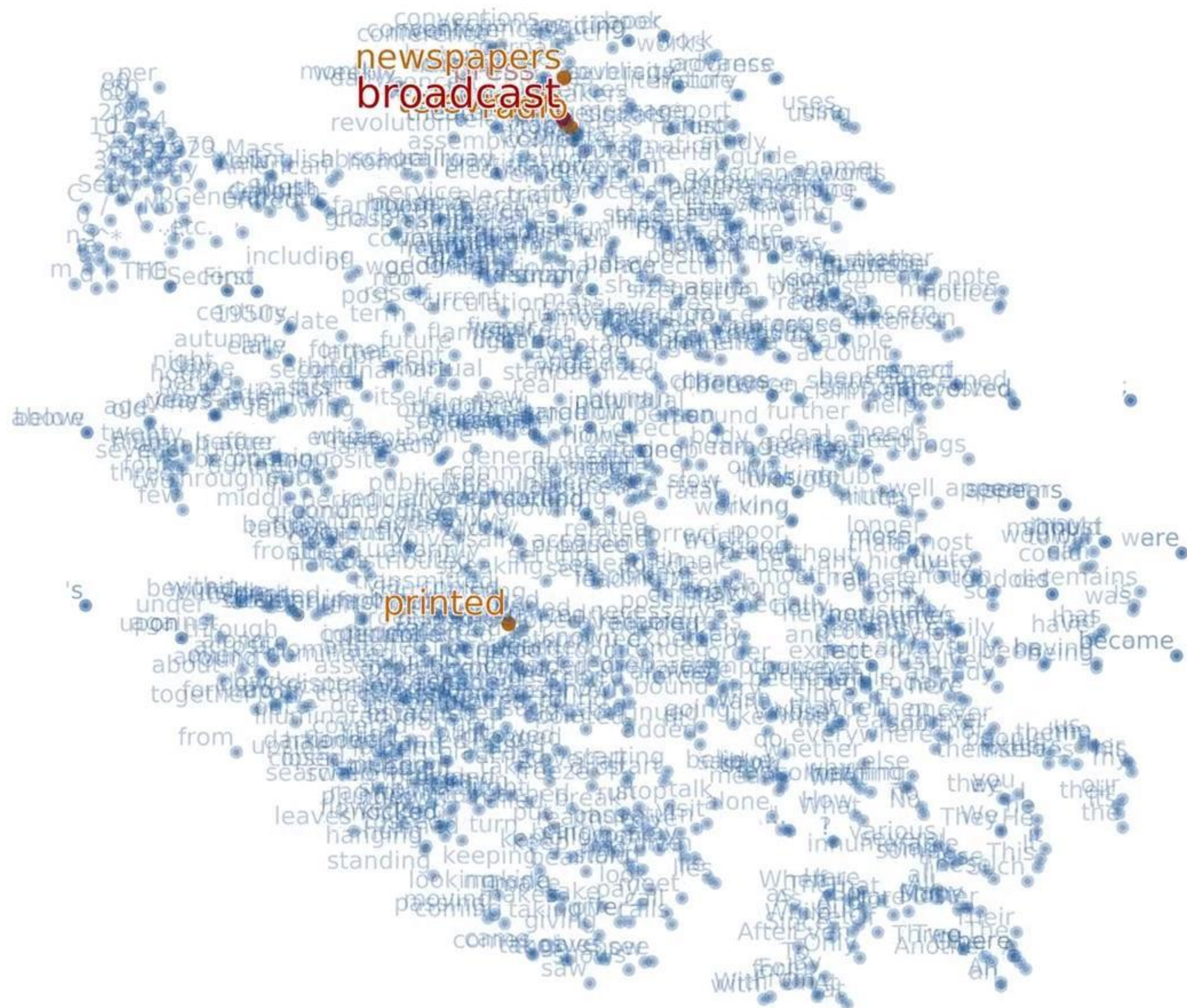
scalable approximate Bayesian inference

# 1989

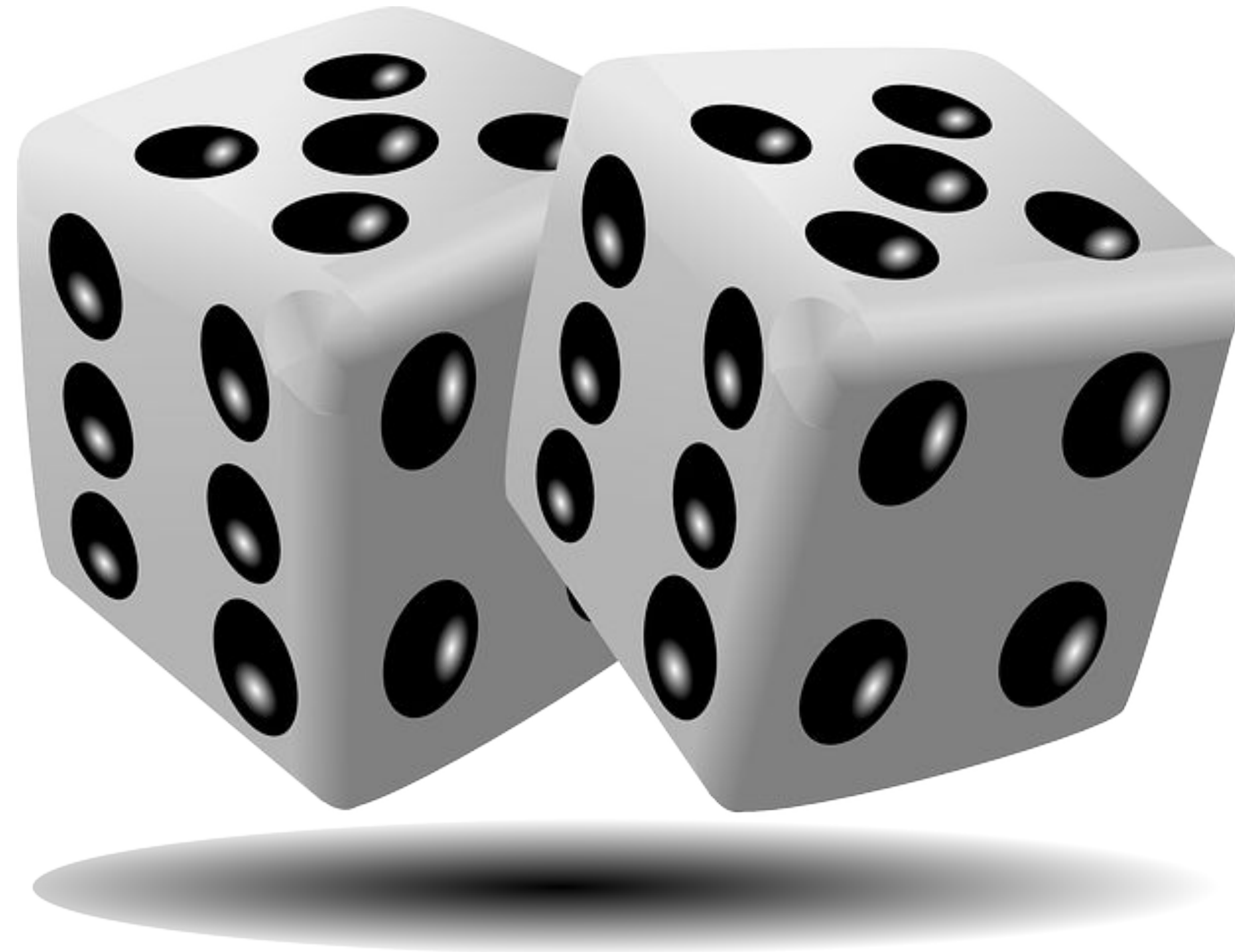
broadcast  
radio

television

TV  
printed  
press



# Bear With Me: Probabilistic Models & Inference



# Probabilistic Models & Bayesian Inference

Notation:  $\mathbf{x}$  = observations (data)  
 $\mathbf{z}$  = latent (i.e., unknown)  
variables that caused  $\mathbf{x}$

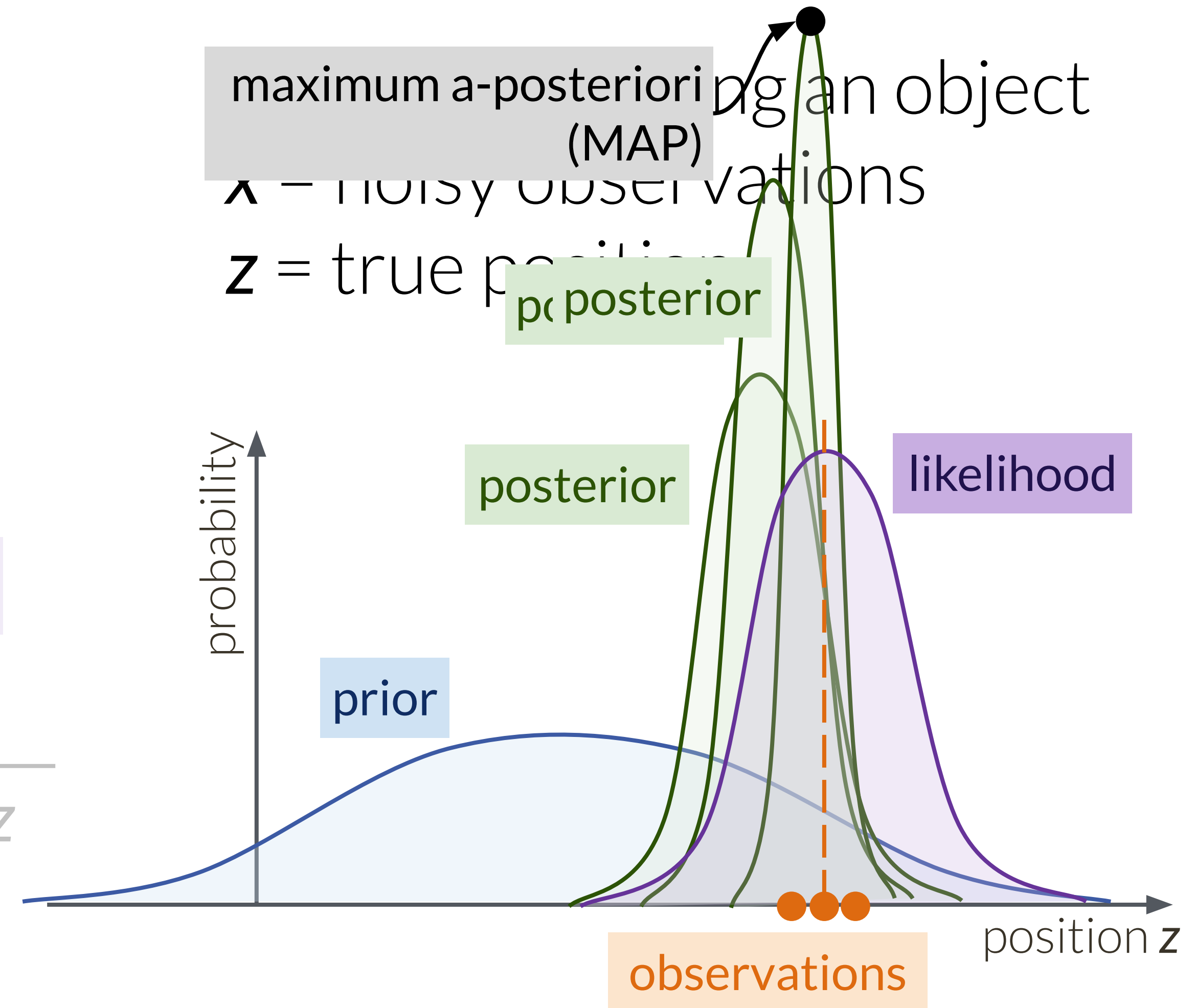
Probabilistic model:  $p(\mathbf{x}, \mathbf{z}) = p(\mathbf{z}) p(\mathbf{x}|\mathbf{z})$

prior

likelihood

Inference: find posterior  $p(\mathbf{z}|\mathbf{x}) = \frac{p(\mathbf{x}, \mathbf{z})}{\int p(\mathbf{x}, \mathbf{z}) d\mathbf{z}}$

probability that latent  
variables  $\mathbf{z}$  explain the  
observed data  $\mathbf{x}$ .



# Example 1: Probabilistic Variant of word2vec

[Barkan AAAI 2017]

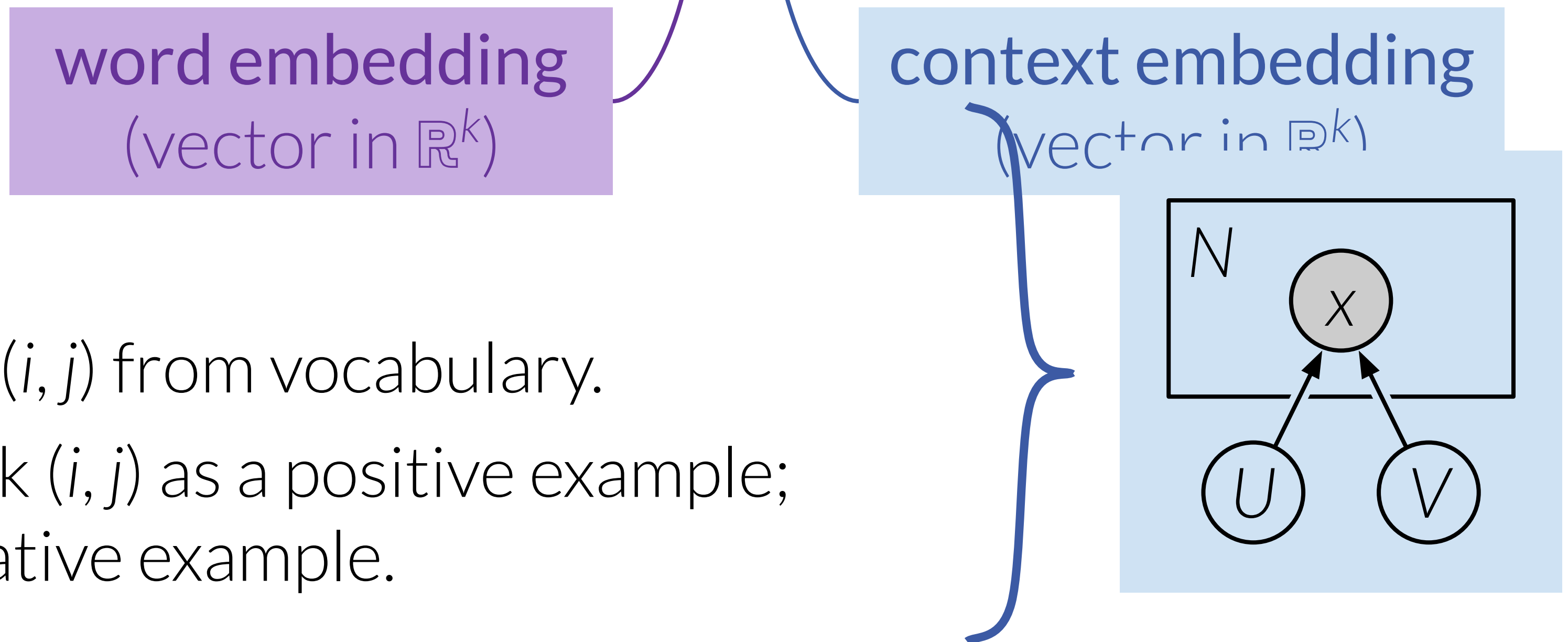
Reminder: word2vec minimizes loss  $\ell = - \sum_{(i,j) \in \text{pos.}} \log \sigma(u_i^\top v_j) - \sum_{(i,j) \in \text{neg.}} \log \sigma(-u_i^\top v_j)$

Observation:  $\ell = - \log p(\mathbf{x}|\mathbf{z})$

Generative process:

*repeat:*

- Draw a random pair of words  $(i, j)$  from vocabulary.
- **With probability  $\sigma(u_i^\top v_j)$ :** mark  $(i, j)$  as a positive example;  
**otherwise:** mark  $(i, j)$  as a negative example.



# Enough Equations, Back to Pretty Pictures

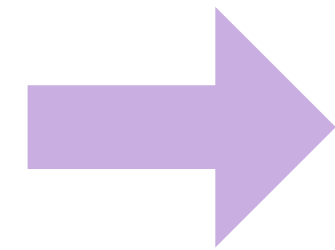
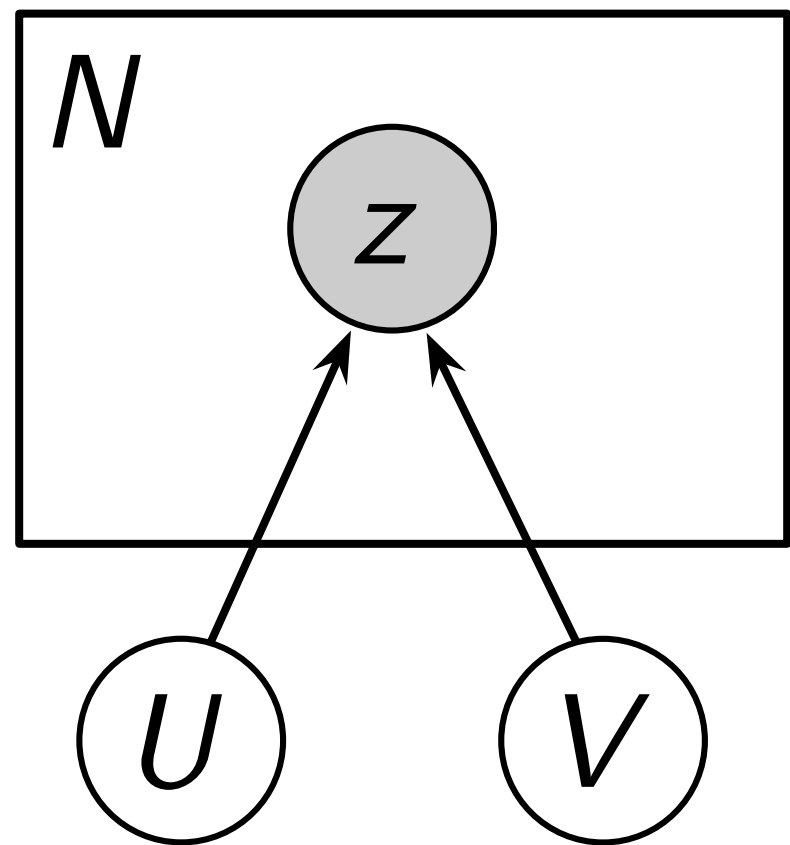


Nymphenburg Park, Munich #nofilter

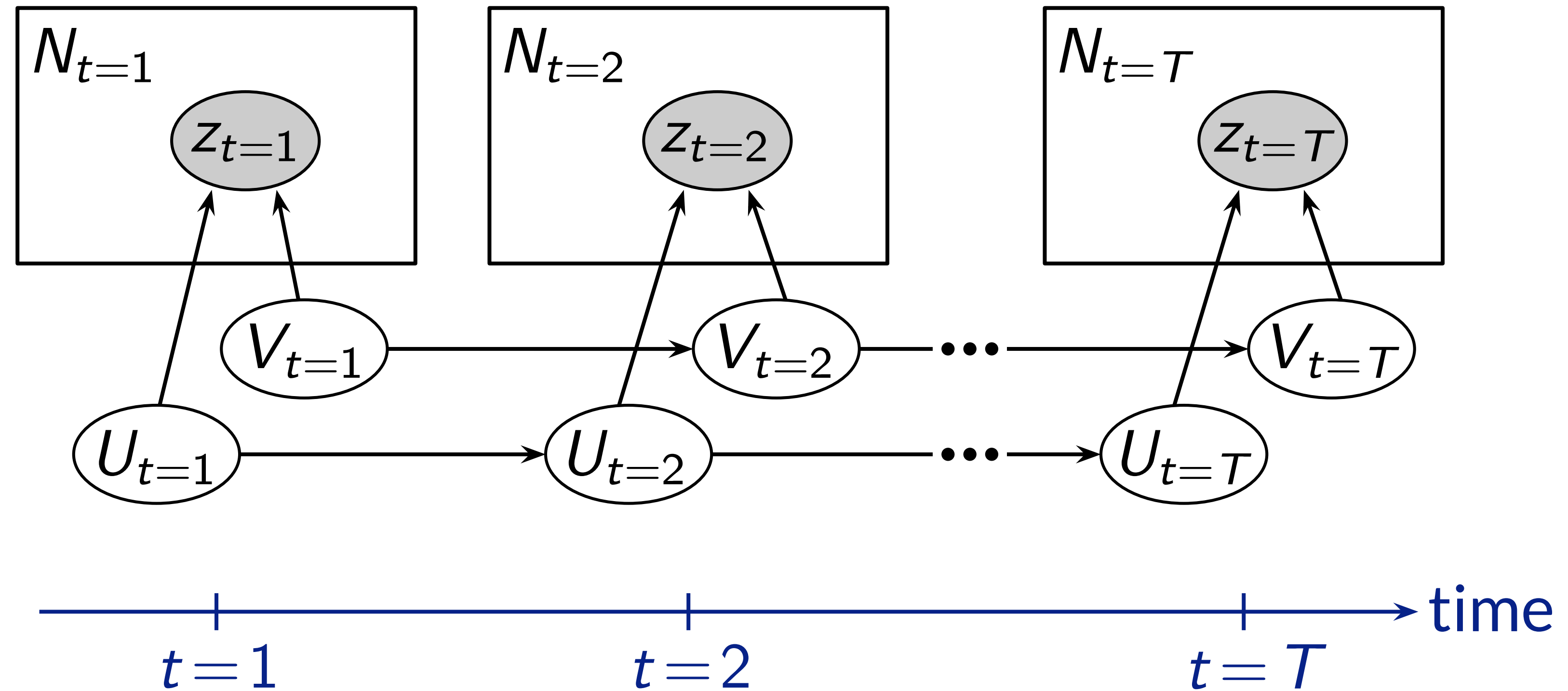
# Dynamic Word Embeddings Model

[Bamler & Mandt, ICML 2017]

static model

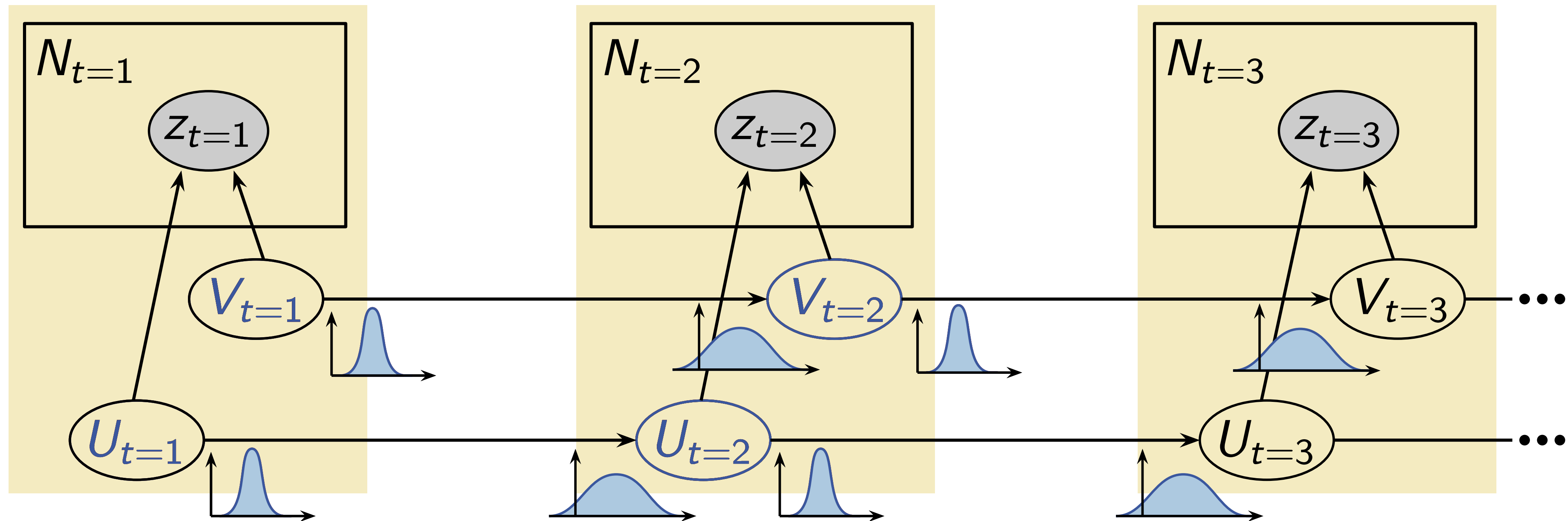


Dynamic Model



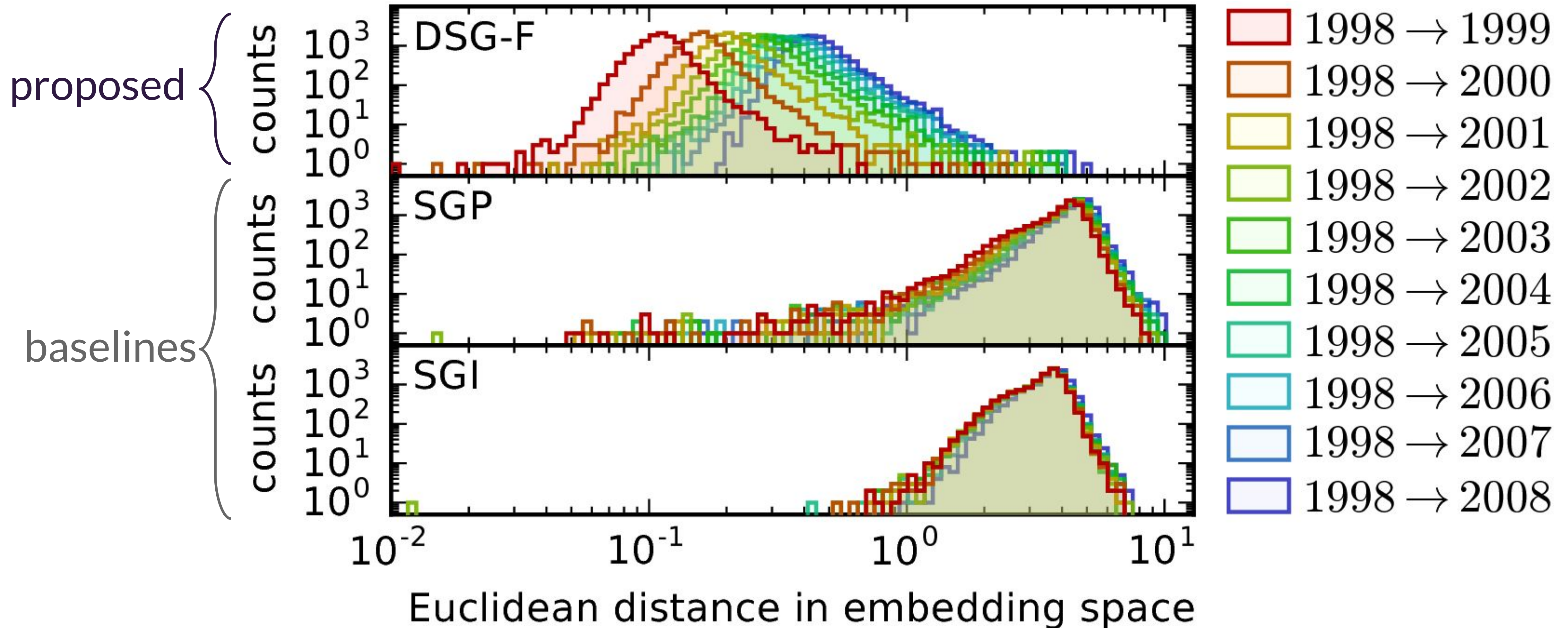
# On-line Learning With Variational Inference

[see “Dynamic Word Embeddings”, Bamler & Mandt, ICML 2017]



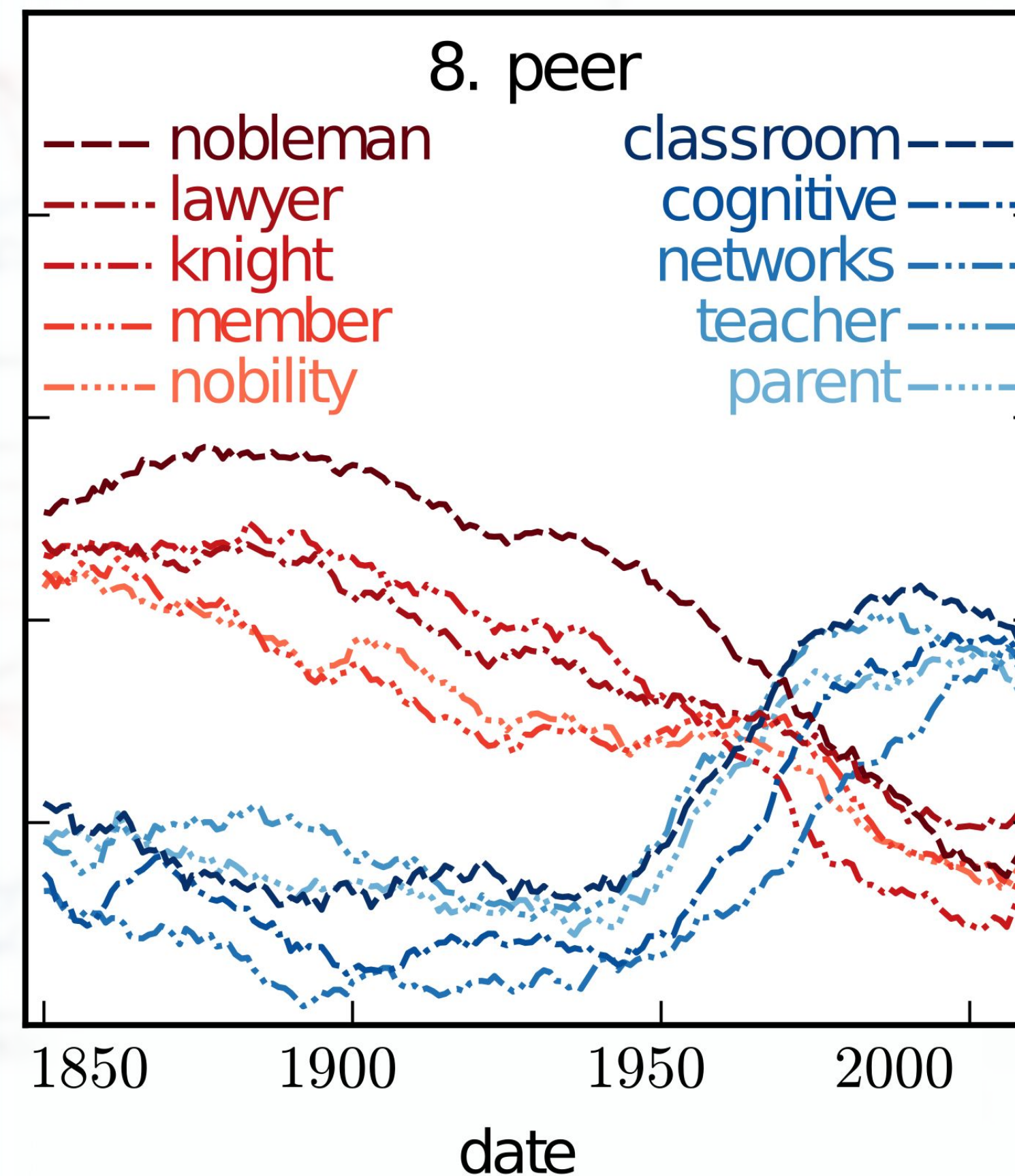
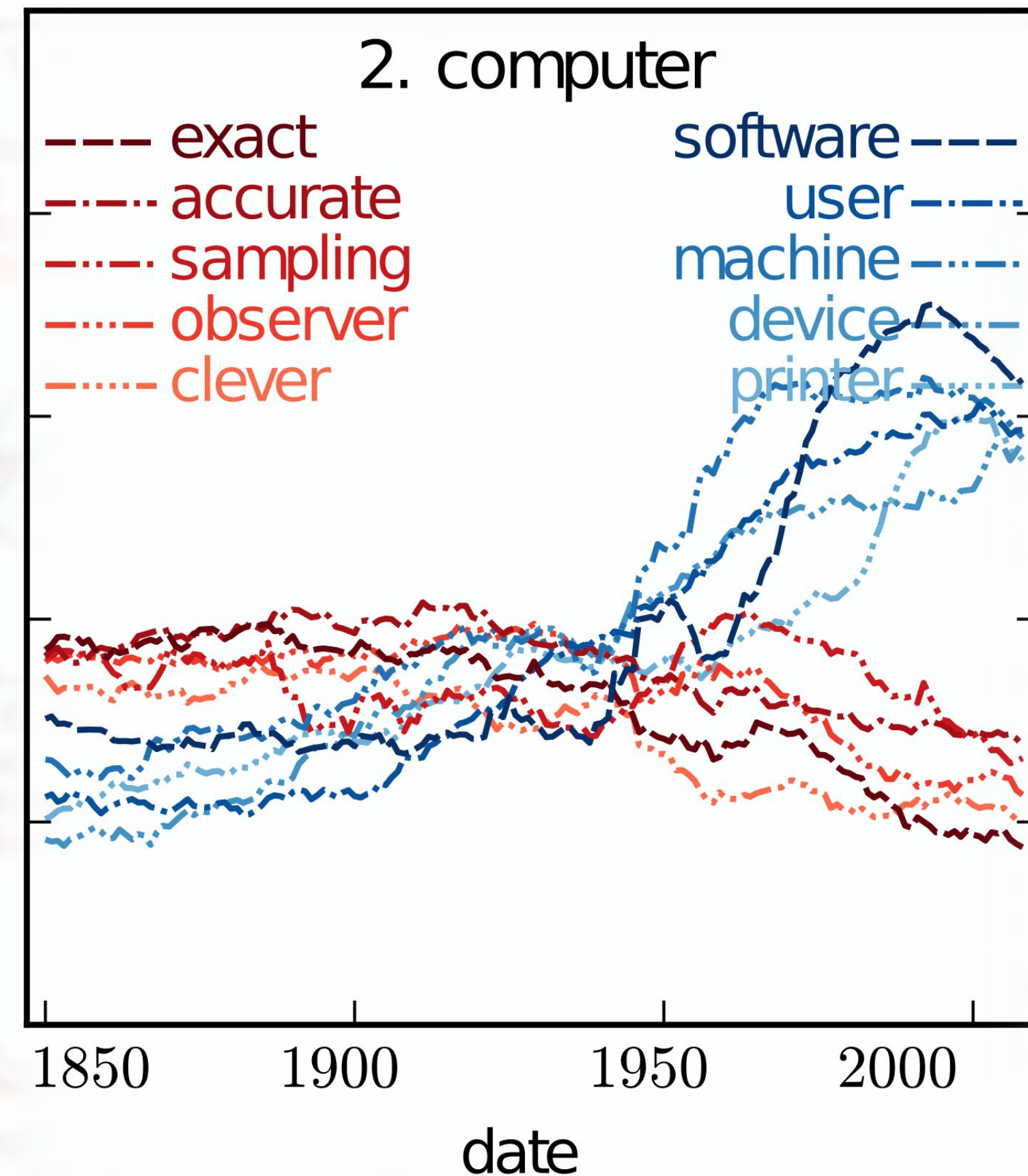
# Results II: Smooth Trajectories in Embedding Space

(Training data: Google Books corpus [Michel et al., 2011])



# Results: Top 10 Most Mobile Words (1850→2008)

(Training data: Google Books corpus [Michel et al., 2011])



# Time Travel

word embeddings  
for year **1800**

word embeddings  
for year **1801**

word embeddings  
for year **2008**



# Results: Word Aging with Goldstone GD

[Bamler & Mandt, ICML 2018]

**2008**

**1800**

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*car*

boat, saddle, canoe, wagon, box

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*DNA*

potassium, chemical, sodium, molecules, displacement

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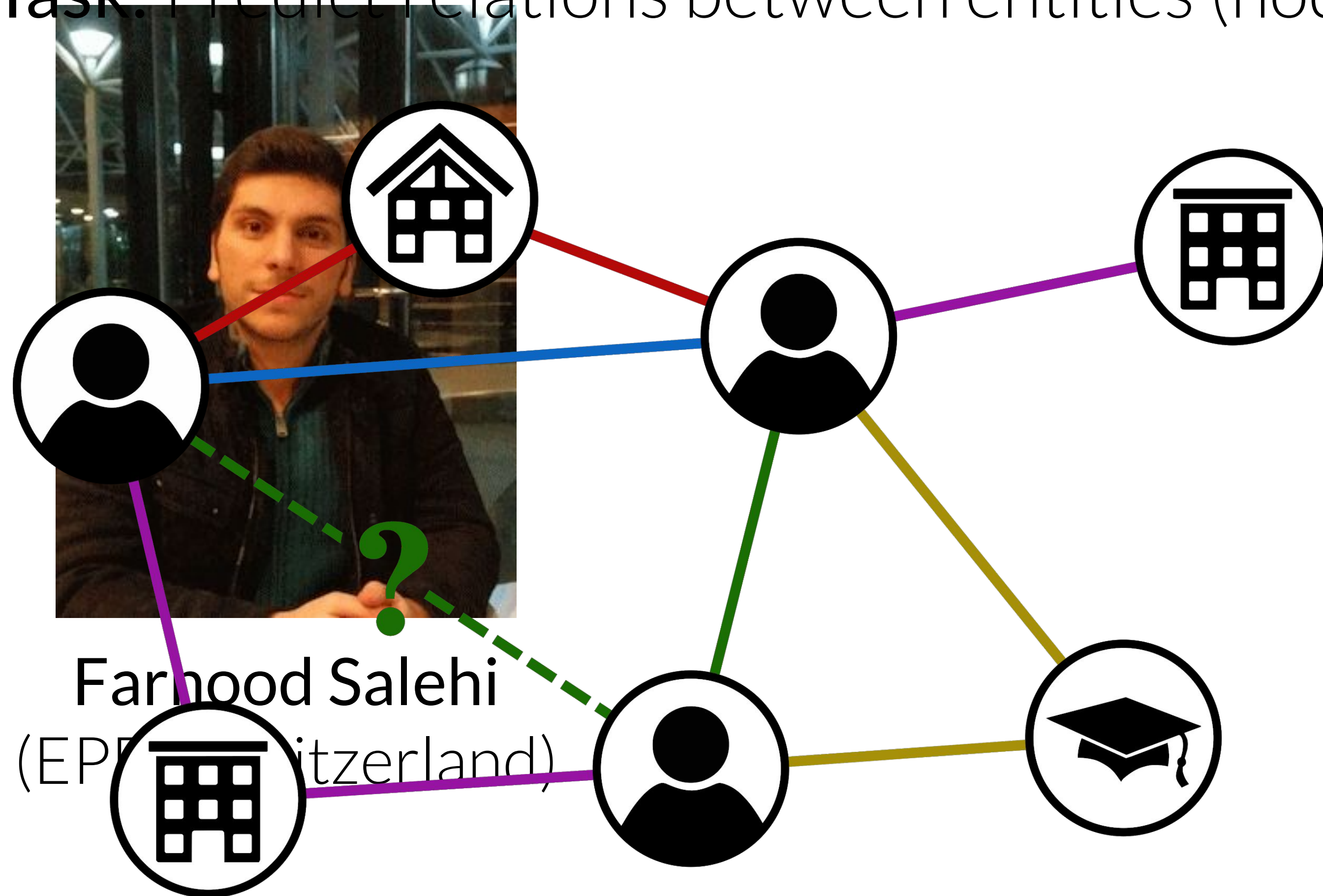
*tuberculosis*

chronic, paralysis, irritation, disease, vomiting

# Example 2: Probabilistic Knowledge Graphs

[Bamler, Salehi & Mandt, UAI 2019]

**Task:** Predict relations between entities (nodes) in a knowledge graph.



Farnood Salehi  
(EPFL, Switzerland)

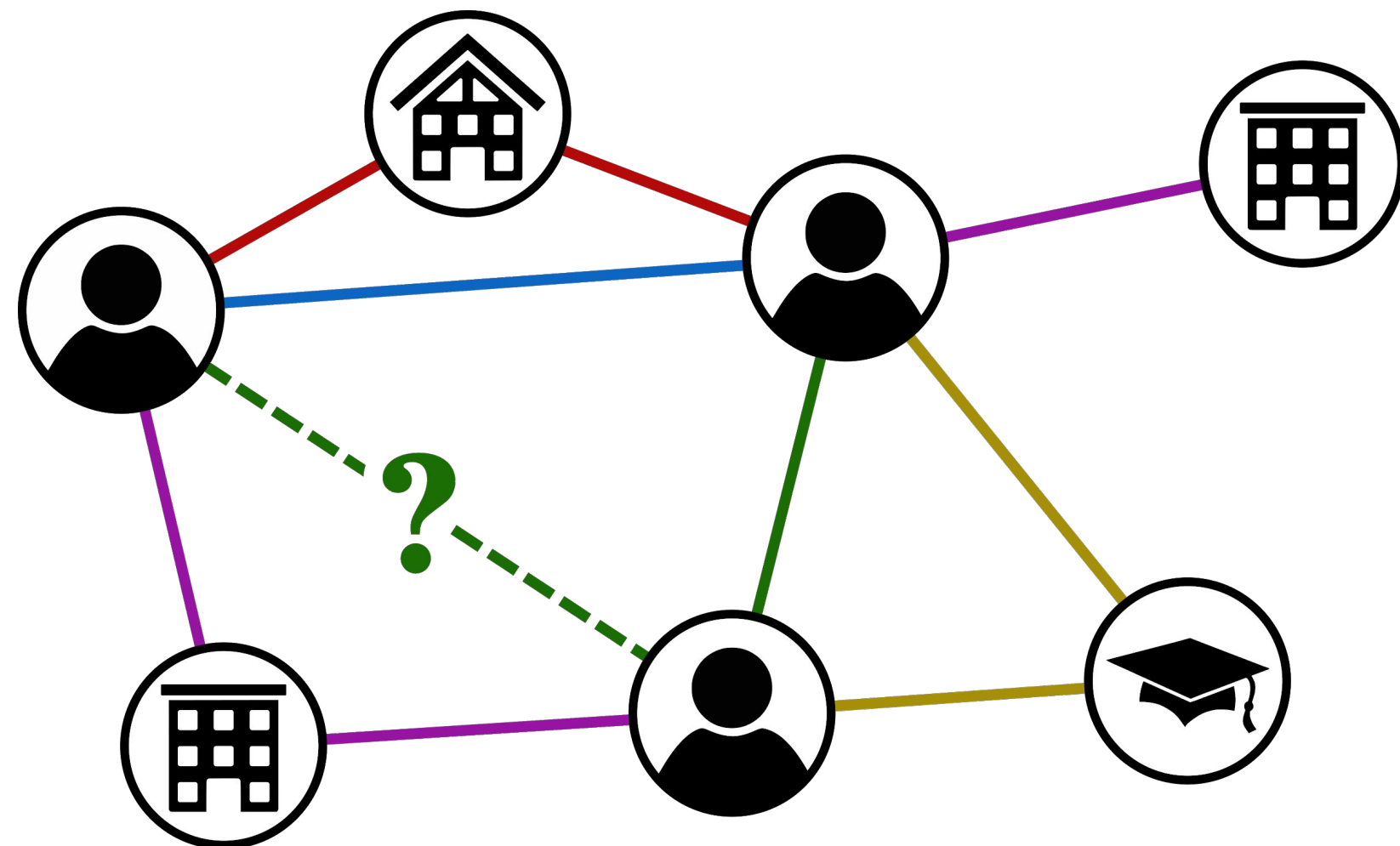
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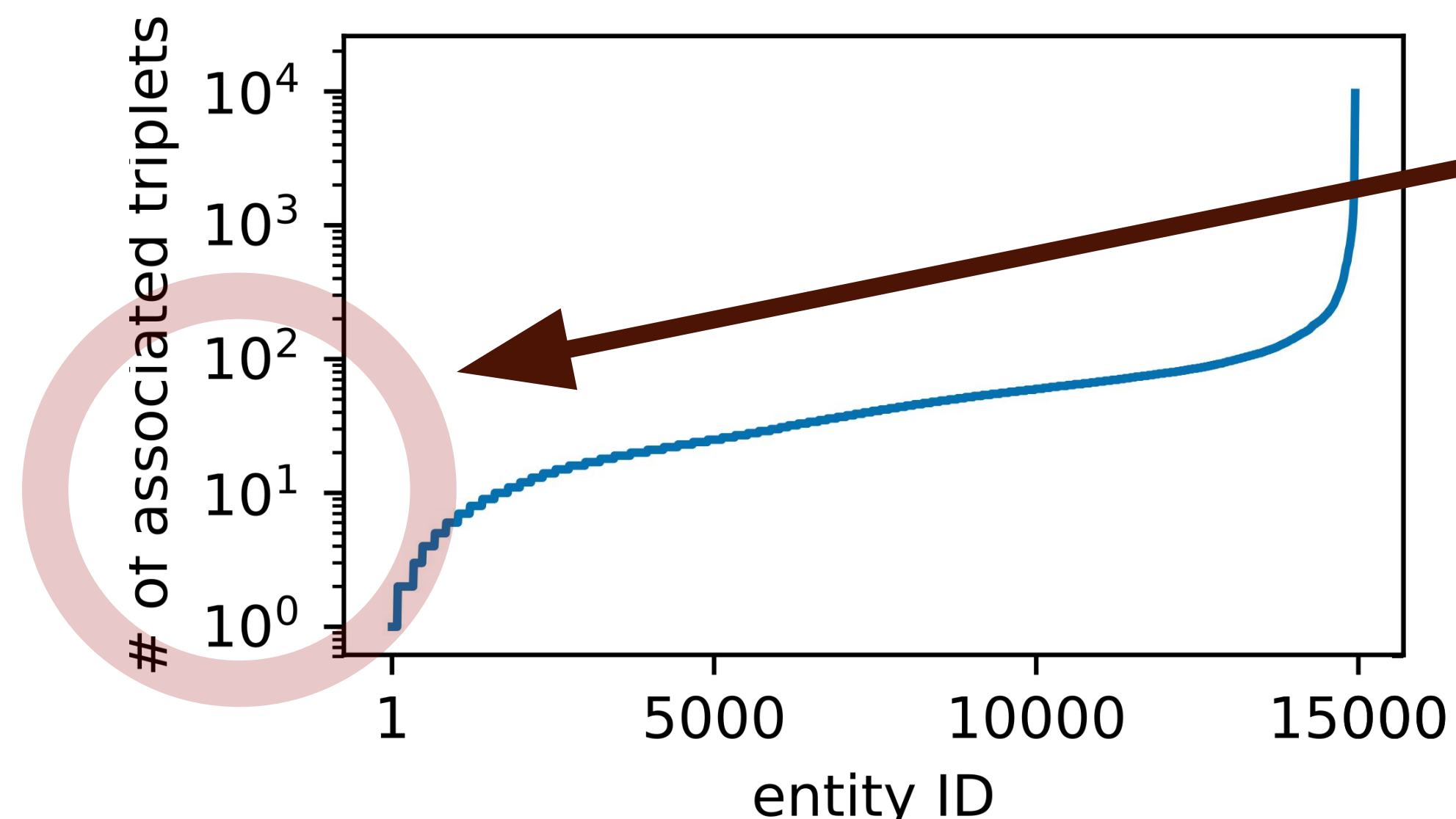
## State of the Art:

Learn embeddings for entities and relation types.



## Problem:

Highly sensitive to hyperparameters  
[Kadlec et al., 2017]



## Reason:

Many entities are supported only by few data points.

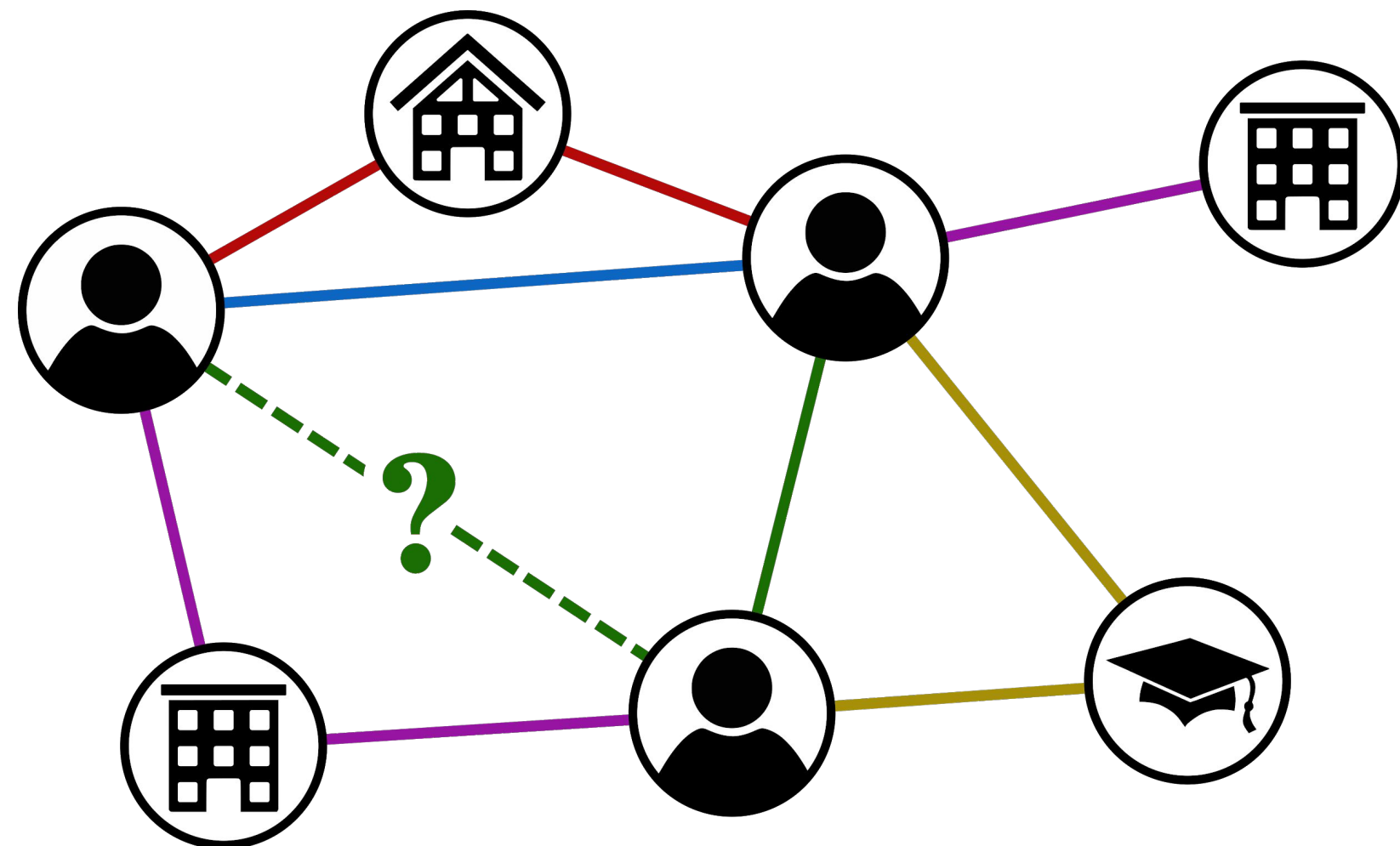
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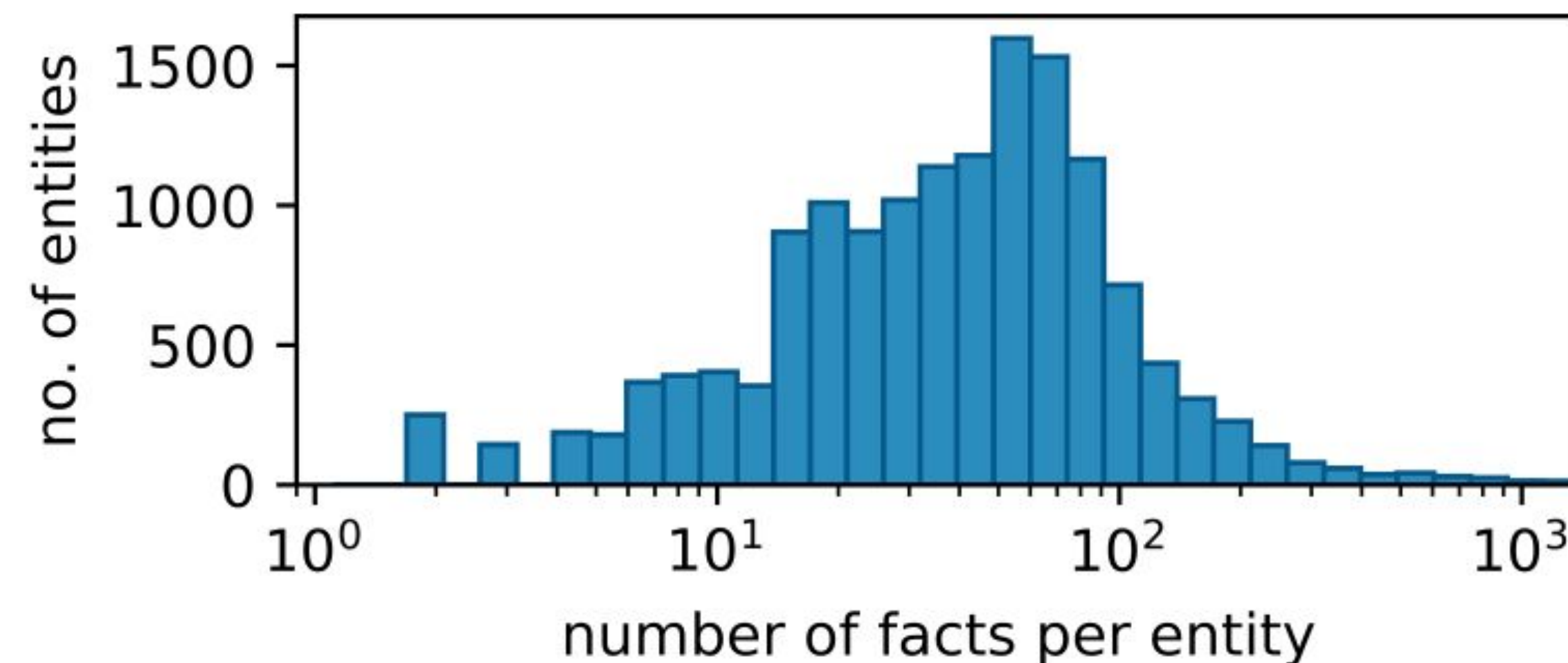
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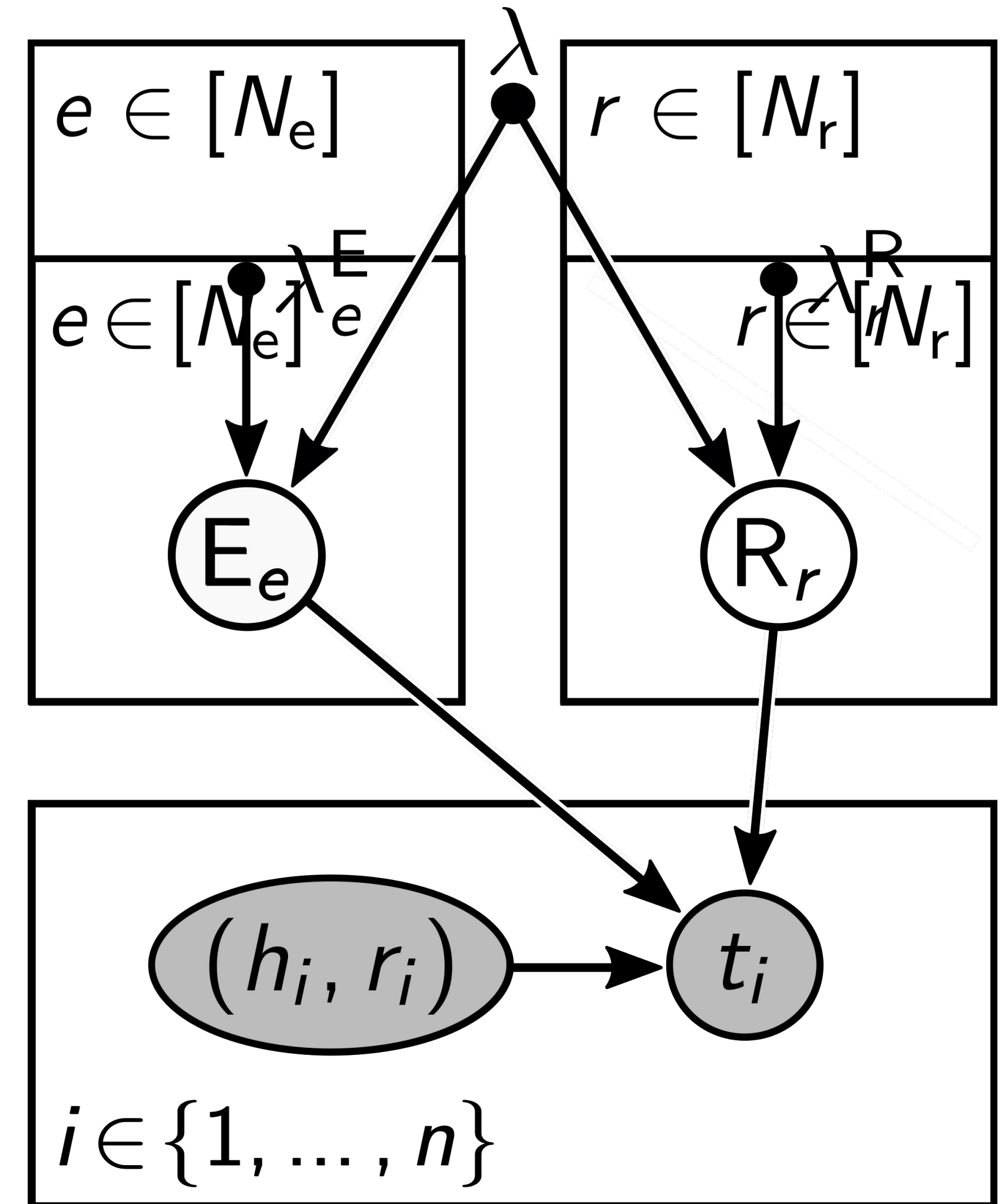


# Example 2: Probabilistic Knowledge Graphs

[Bamler, Salehi & Mandt, UAI 2019]

## Our Solution:

- Reinterpret existing models as **probabilistic generative models** of relational facts (*head*, *relation*, *tail*).
- Introduce macroscopic number of *local* hyperparameters (**> 10,000**).
- Tune hyperparameters efficiently with **variational expectation maximization**.



# Results: Probabilistic Knowledge Graph Embeddings

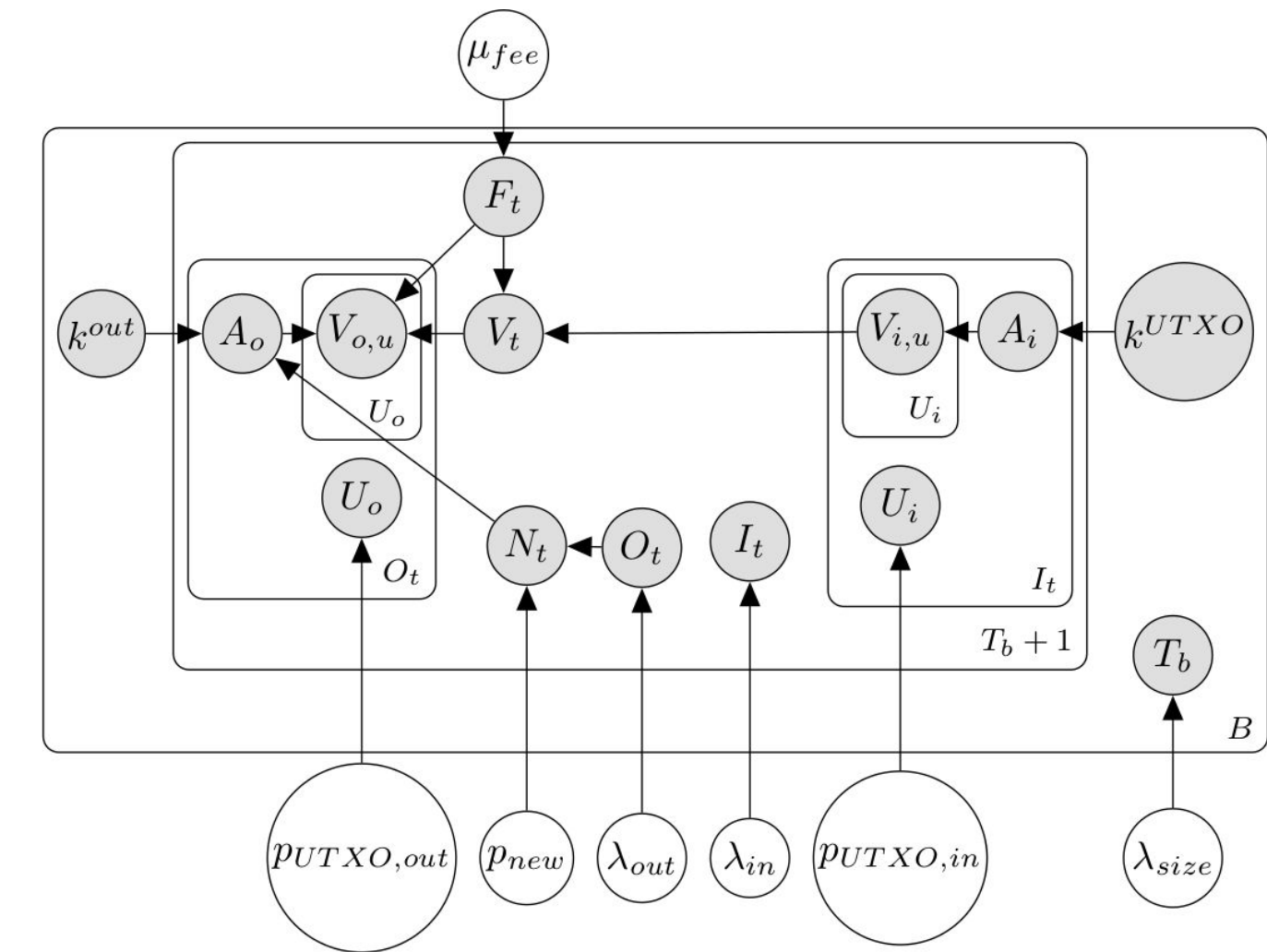
[Bamler, Salehi & Mandt, UAI 2019]

Link prediction outperforms previous state of the art.

↓ model	↓ variant	data set → metric →	WN18RR		WN18		FB15K-237		FB15K	
			MRR	Hits@10	MRR	Hits@10	MRR	Hits@10	MRR	Hits@10
DistMult	Yang et al. [2015] (orig.)		–	–	0.83	0.942	–	–	0.35	0.577
DistMult	Kadlec et al. [2017]		–	–	0.790	0.950	–	–	0.837	0.904
DistMult	Dettmers et al. [2018]		0.43	0.49	0.822	0.936	0.241	0.419	0.654	0.824
DistMult	Ours (after variational EM)		<b>0.455</b>	<b>0.544</b>	<b>0.911</b>	<b>0.961</b>	<b>0.357</b>	<b>0.548</b>	<b>0.841</b>	<b>0.914</b>
ComplEx	Trouillon et al. [2016] (orig.)		–	–	0.941	0.947	–	–	0.692	0.840
ComplEx	Lacroix et al. [2018]*		0.478	0.569	0.952	0.963	0.364	0.555	<b>0.857</b>	0.909
ComplEx	Ours (after variational EM)		<b>0.486</b>	<b>0.579</b>	<b>0.953</b>	<b>0.964</b>	<b>0.365</b>	<b>0.560</b>	0.854	<b>0.915</b>

# Discussion: Embedding the Blockchain

- ▶ **Analogy to knowledge graphs:**  
transaction  $\approx$  relational fact; token  $\approx$  relation
- ▶ **Temporal component:**  
 $\approx$  Dynamic Word Embeddings, but more ephemeral.
- ▶ **Analysis (ideas):**
  - ▷ semantic analysis of users & tokens using embeddings
  - ▷ predict transactions?
- ▶ **Action Items:**
  - ▷ *Get a data set.*
  - ▷ Discuss existing literature.
  - ▷ Come up with more concrete analysis questions (maybe as we look at the data).



[Jourdan et al., 2019]